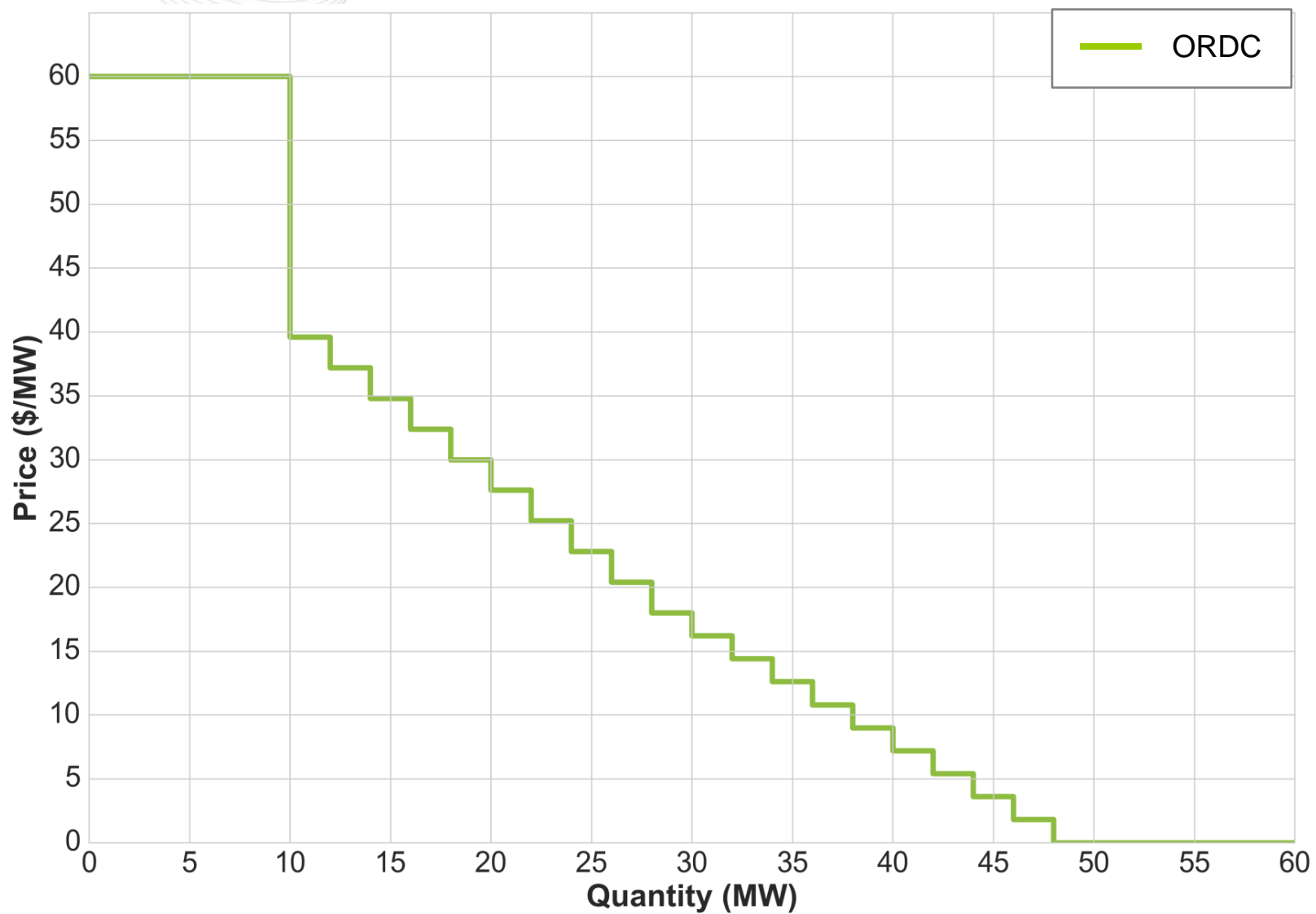


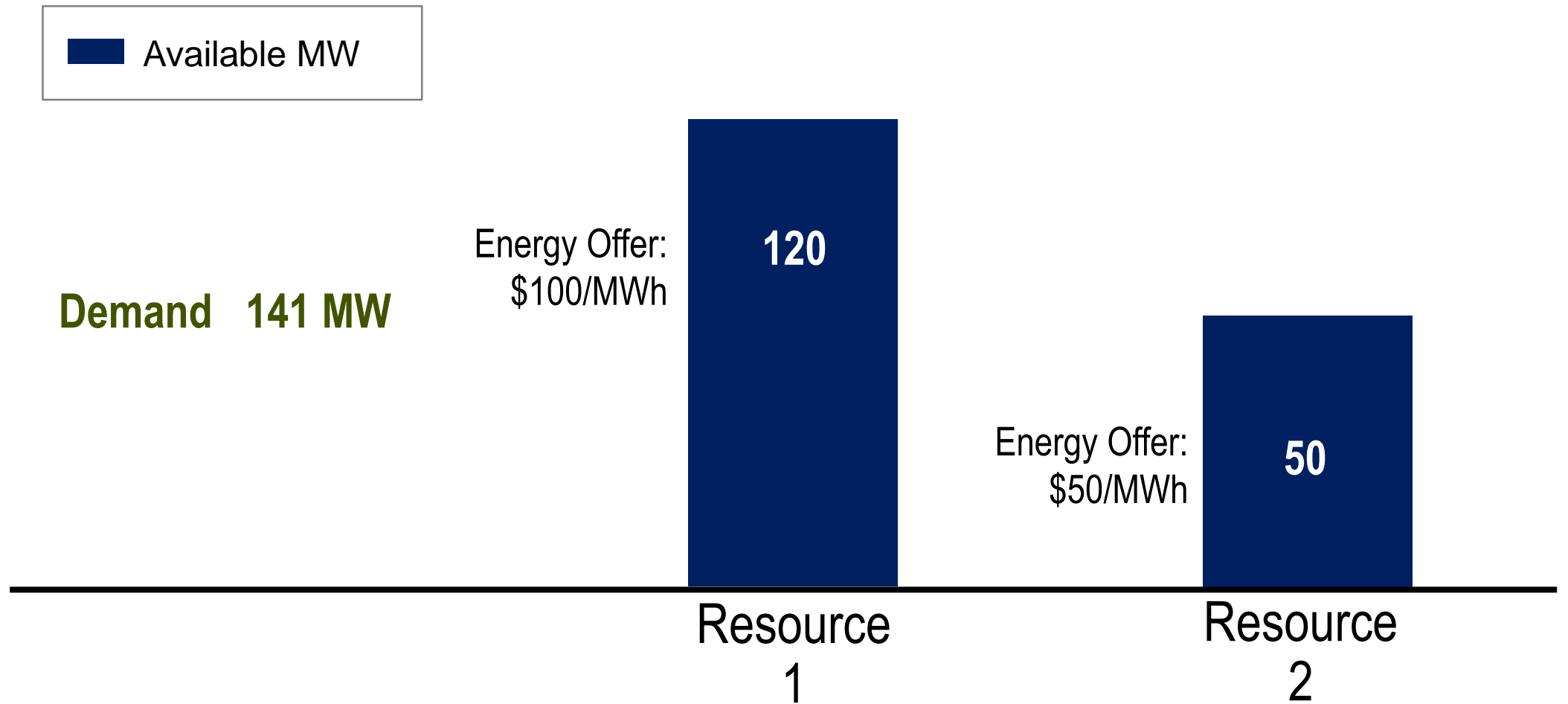
Energy and Reserves Co-Optimization Examples

EPFSTF

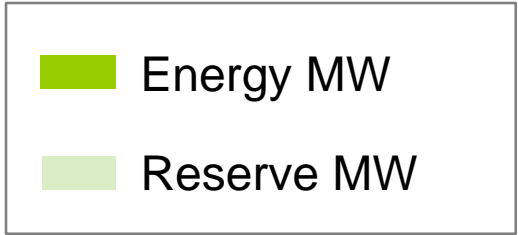
August 26, 2021



Example #1: Capacity Constrained



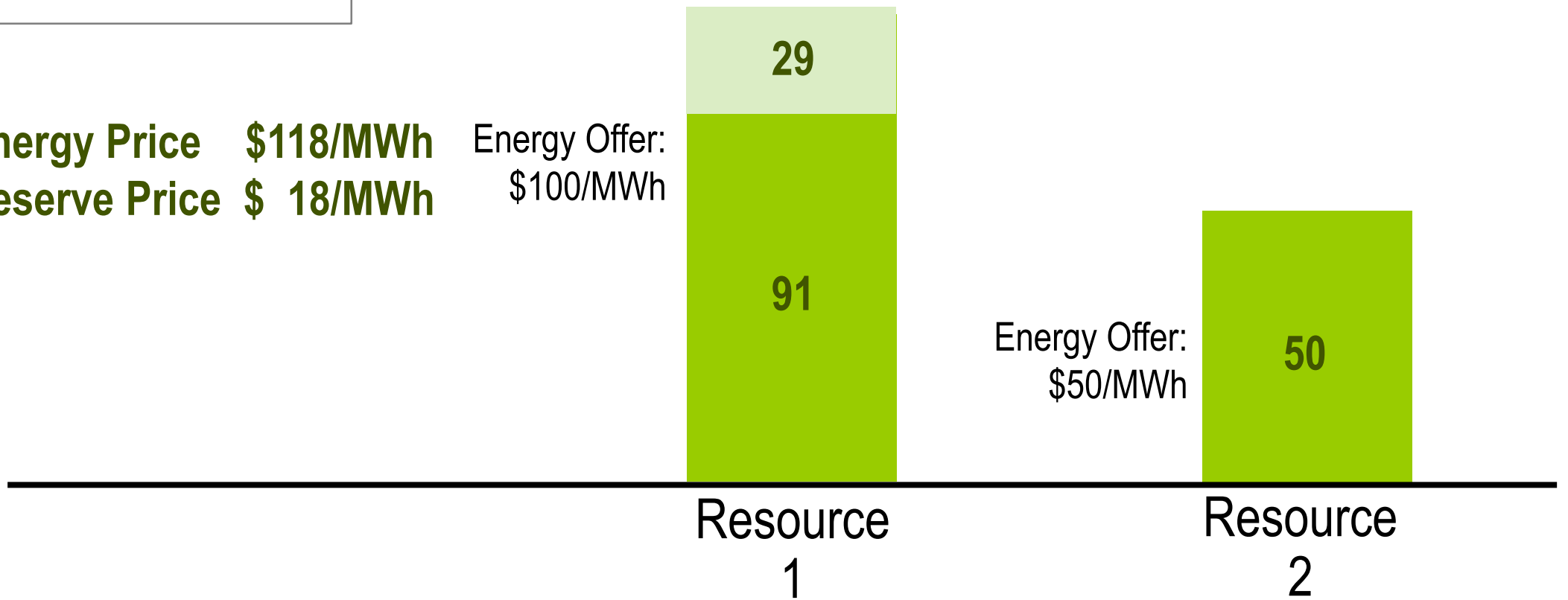
Example #1: Results



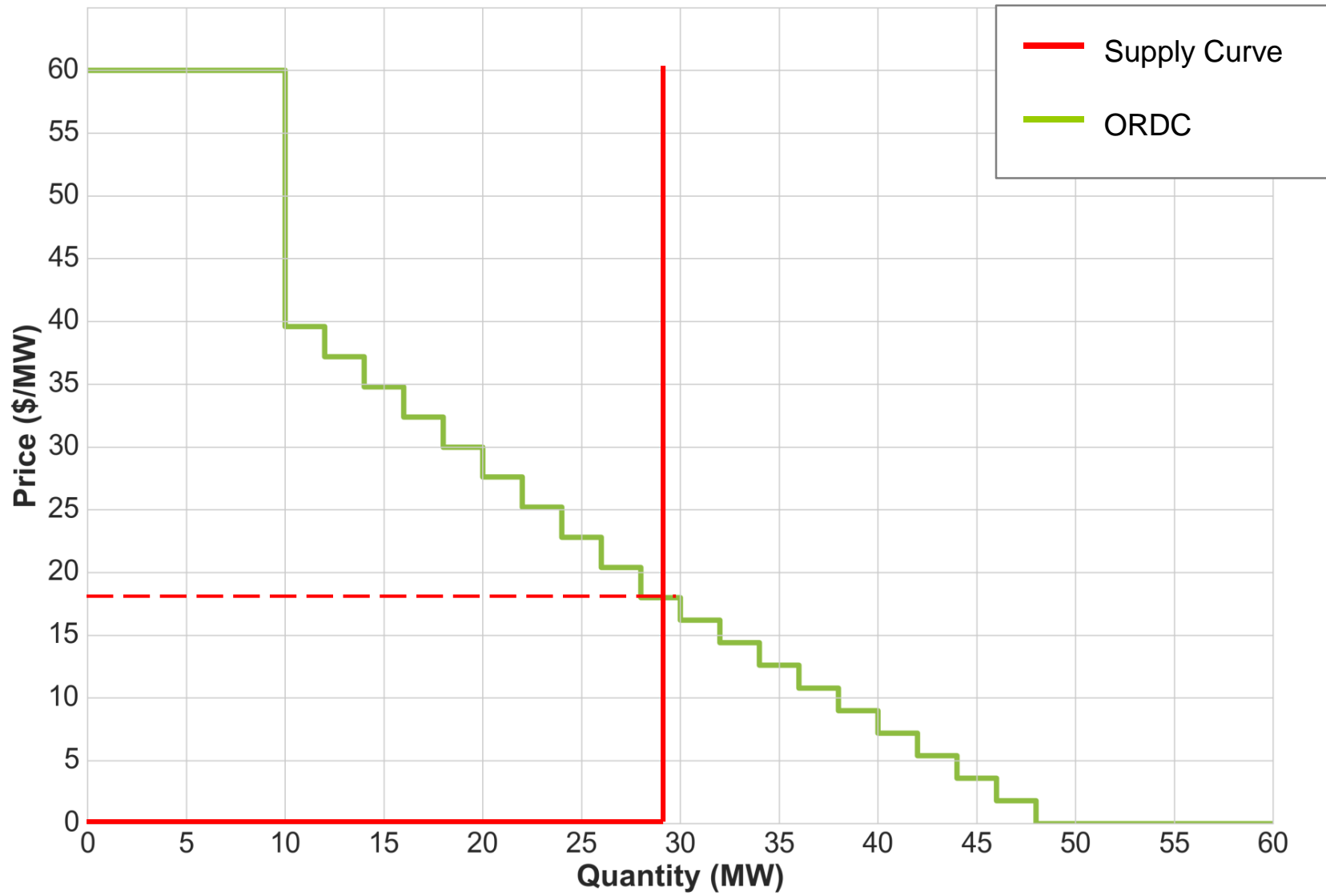
Energy Price \$118/MWh
Reserve Price \$ 18/MWh

Energy Offer:
 \$100/MWh

Demand 141 MW



Example #1: Results - ORDC



Co-Optimizing Energy and Reserves – Example 1

Objective Function = cost to produce energy + cost to produce reserve – willing to pay for reserve

$$\begin{aligned} \text{Objective Function} &= (\$50/\text{MW} \times 50 \text{ MW}) + (\$100/\text{MW} \times 91 \text{ MW}) + (\$0 \text{ MW} \times 29 \text{ MW}) - \$1158 \\ &= \mathbf{\$10,442} \end{aligned}$$

If we need to serve 1 MW of additional energy:

$$\begin{aligned} \text{Objective Function (+1MW)} &= (\$50/\text{MW} \times 50 \text{ MW}) + (\$100/\text{MW} \times \mathbf{92 \text{ MW}}) + (\$0/\text{MW} \times \mathbf{28 \text{ MW}}) - \$1140 \\ &= \mathbf{\$10,560} \end{aligned}$$

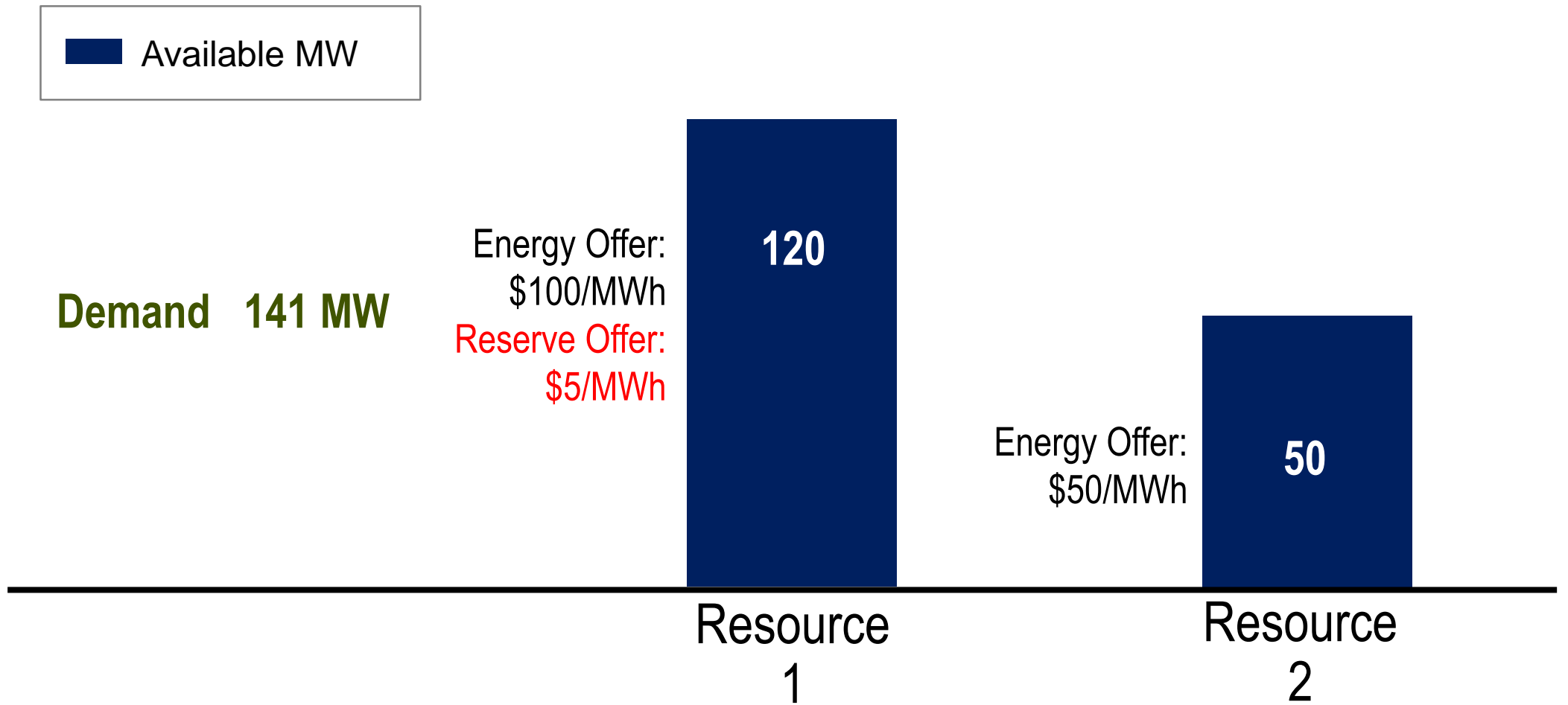
The change in the Objective function to serve 1 MW of additional energy is:

$$\begin{aligned} \text{Change in Objective Function} &= \$10,560 - \$10,442 \\ &= \$118 \end{aligned}$$

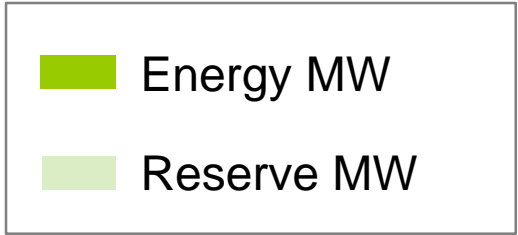
Therefore, the energy clearing price is \$118/MWh. Note that, **for this particular example**, the reserve price (\$18/MWh) ends up being added to the original energy-only price (\$100/MWh)

Resource 1 is indifferent to providing energy or reserves due to the co-optimization of energy and reserves

Example #2: Capacity Constrained with Reserve Offer



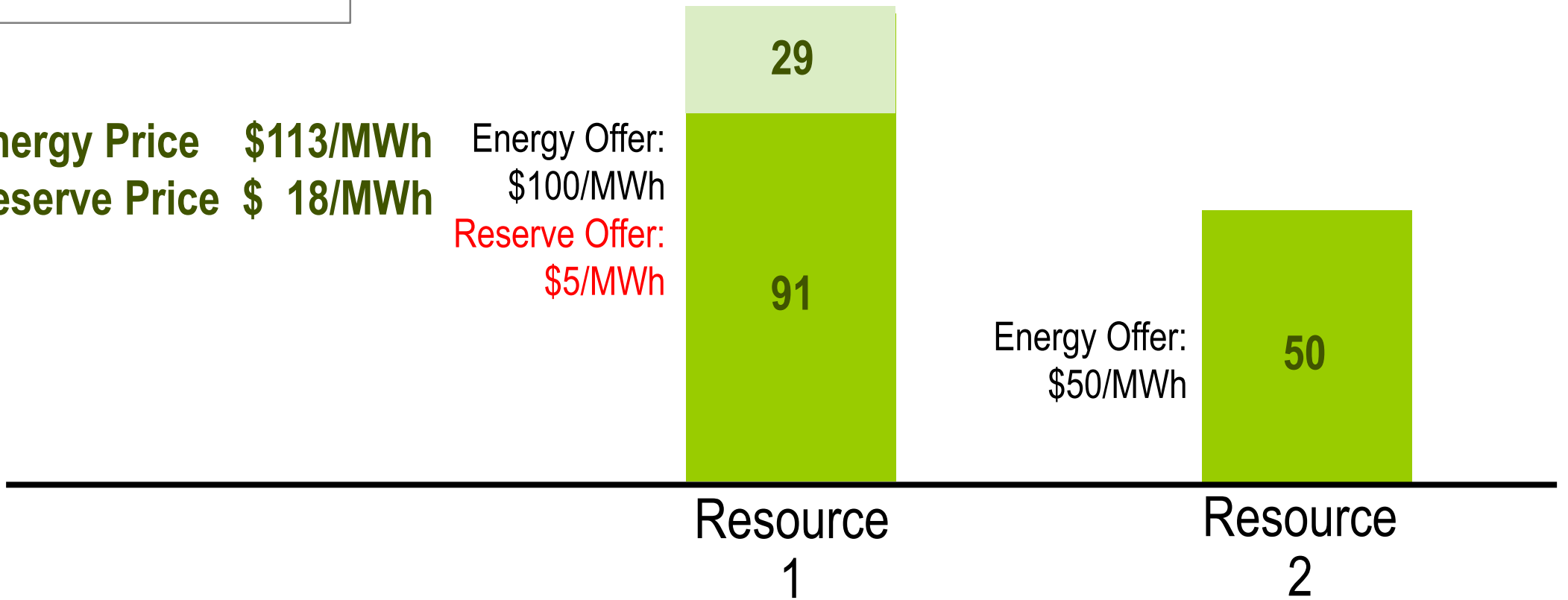
Example #2: Results



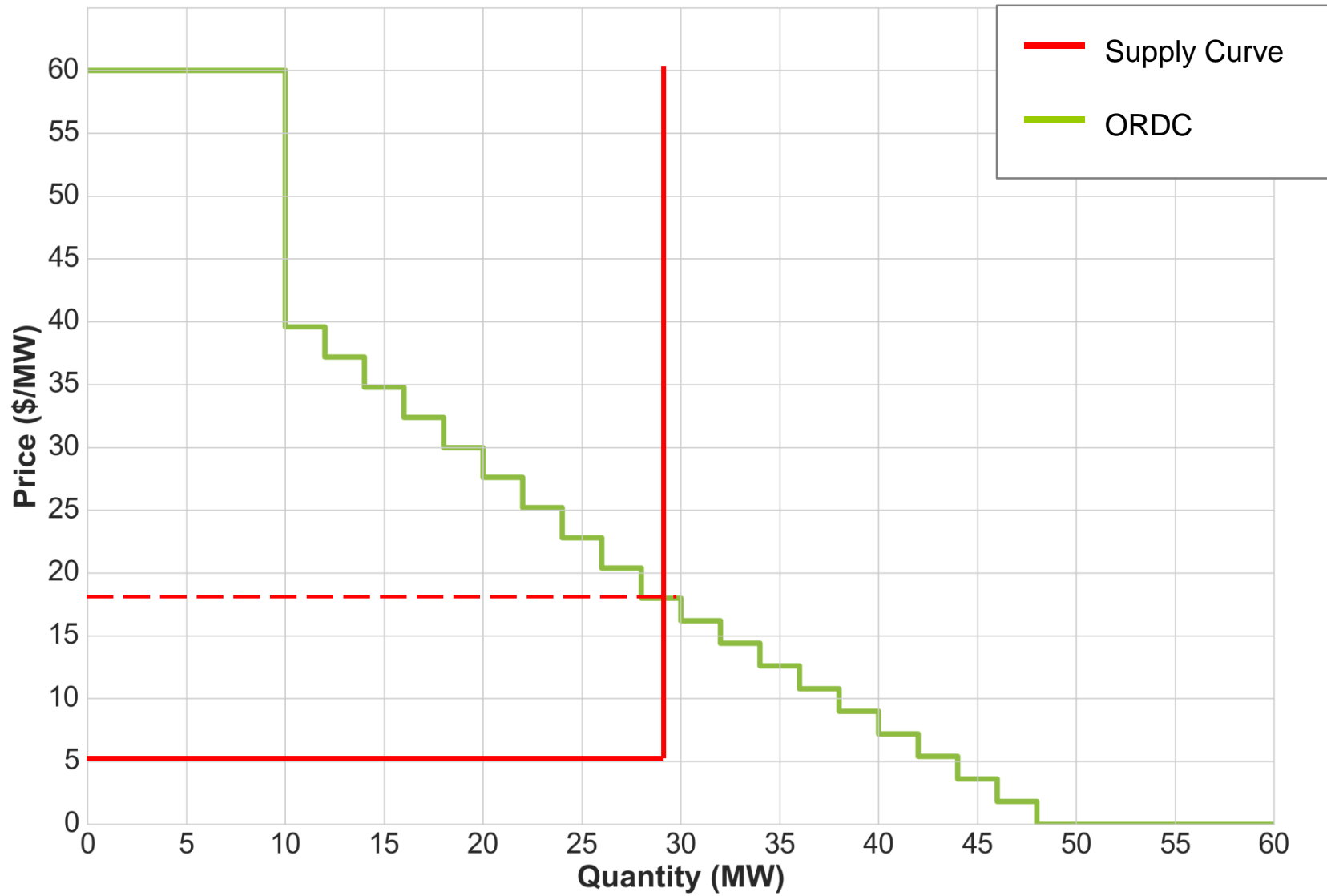
Demand 141 MW

Energy Price \$113/MWh
Reserve Price \$ 18/MWh

Energy Offer:
 \$100/MWh
 Reserve Offer:
 \$5/MWh



Example #2: Results - ORDC



Co-Optimizing Energy and Reserves – Example 2

Objective Function = cost to produce energy + cost to produce reserve – willing to pay for reserve

$$\begin{aligned} \text{Objective Function} &= (\$50/\text{MW} \times 50 \text{ MW}) + (\$100/\text{MW} \times 91 \text{ MW}) + (\$5 \text{ MW} \times 29 \text{ MW}) - \$1158 \\ &= \mathbf{\$10,587} \end{aligned}$$

If we need to serve 1 MW of additional energy:

$$\begin{aligned} \text{Objective Function (+1MW)} &= (\$50/\text{MW} \times 50 \text{ MW}) + (\$100/\text{MW} \times \mathbf{92 \text{ MW}}) + (\$5 \text{ MW} \times \mathbf{28 \text{ MW}}) - \$1140 \\ &= \mathbf{\$10,700} \end{aligned}$$

The change in the Objective function to serve 1 MW of additional energy is:

$$\begin{aligned} \text{Change in Objective Function} &= \$10,700 - \$10,587 \\ &= \$113 \end{aligned}$$

Therefore, the energy clearing price is \$113/MWh. Note that, **for this particular example**, the benefit to the system (\$13/MWh) ends up being added to the original energy-only price (\$100/MWh)

Resource 1 is indifferent to providing energy or reserves due to the co-optimization of energy and reserves

Example #3: Ramp Constrained

■ Available MW

Demand 141 MW

Energy Offer:
\$100/MWh
Reserve Limit:
15 MW



Energy Offer:
\$50/MWh



Resource
1

Resource
2

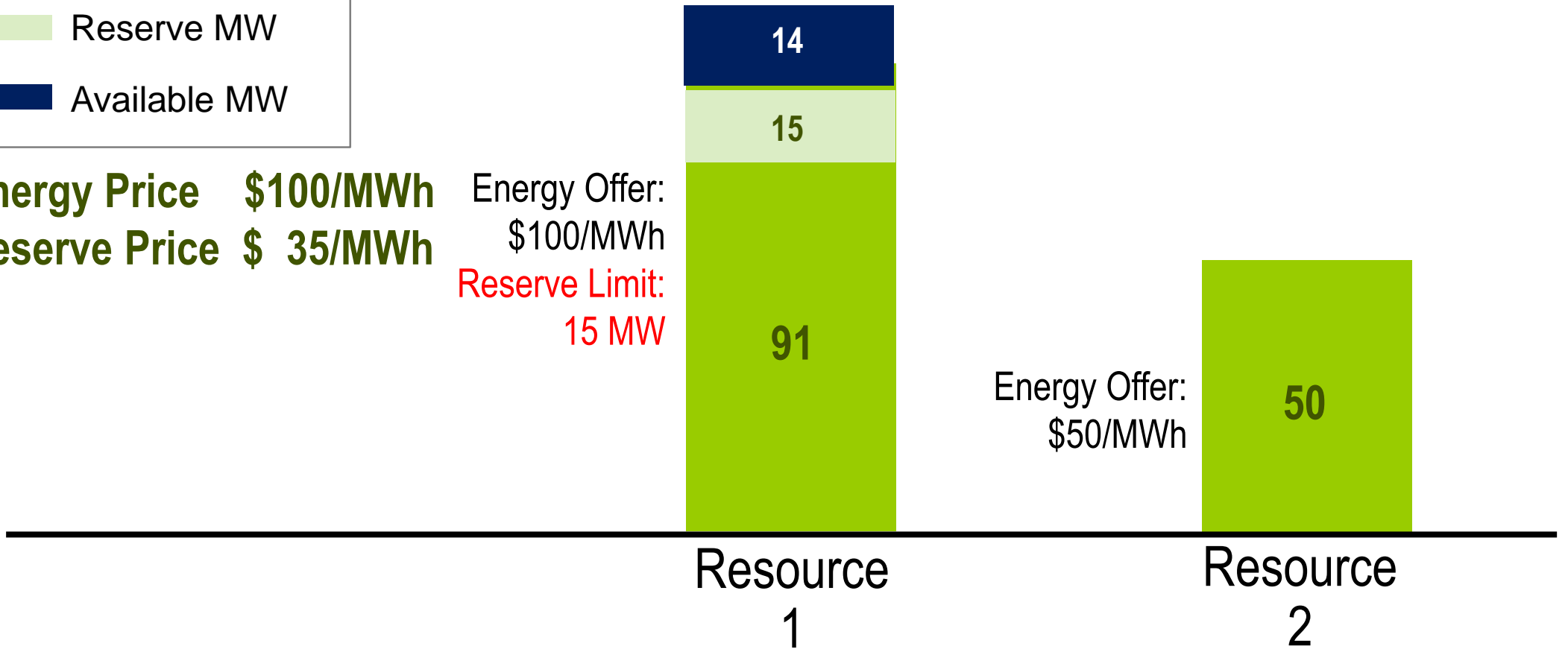
Example #3: Results



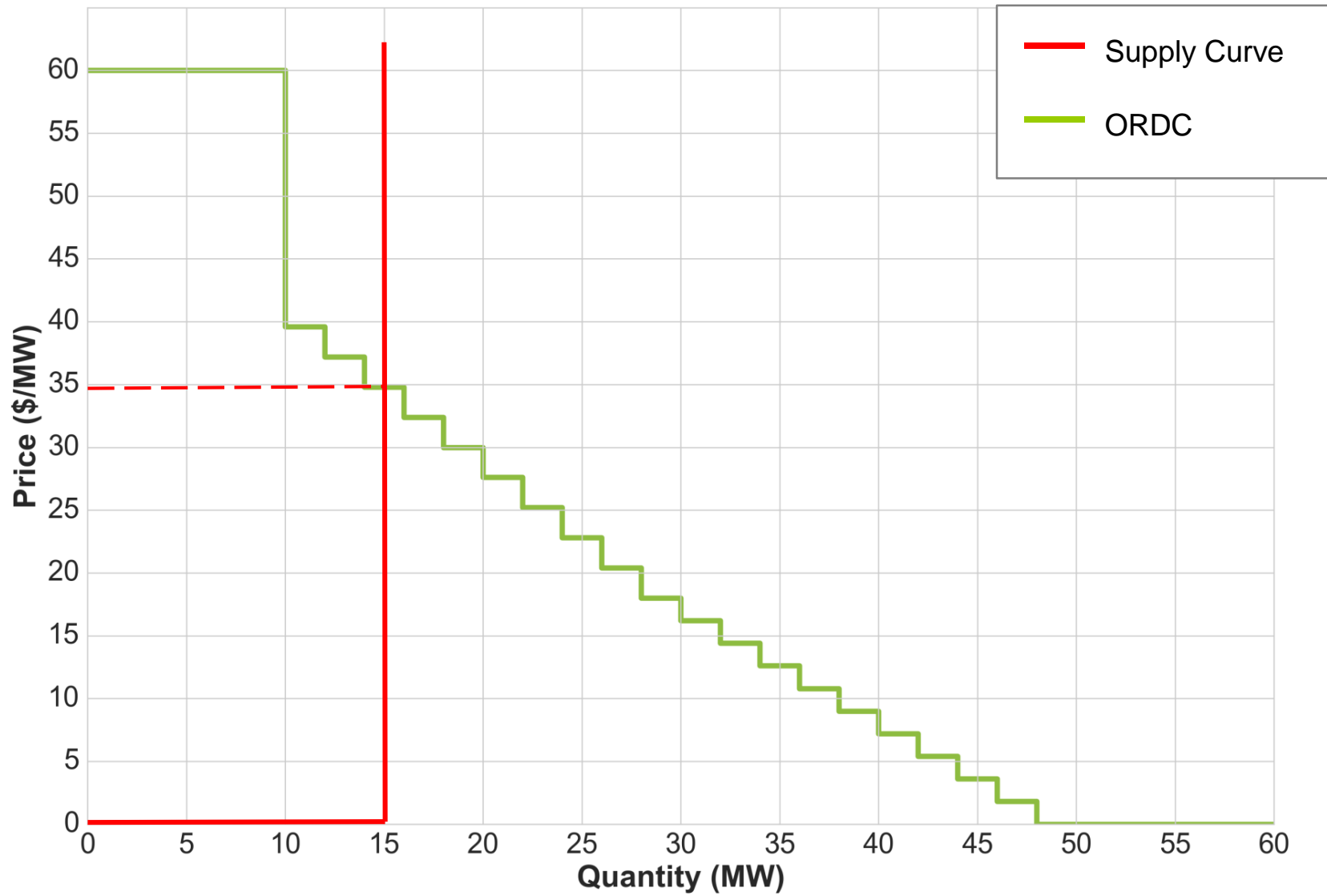
Energy Price \$100/MWh
Reserve Price \$ 35/MWh

Energy Offer: \$100/MWh
Reserve Limit: 15 MW

Demand 141 MW



Example #3: Results - ORDC



Co-Optimizing Energy and Reserves – Example 3

Objective Function = cost to produce energy + cost to produce reserve – willing to pay for reserve

$$\begin{aligned} \text{Objective Function} &= (\$50/\text{MW} \times 50 \text{ MW}) + (\$100/\text{MW} \times 91 \text{ MW}) + (\$0 \text{ MW} \times 15 \text{ MW}) - \$790 \\ &= \mathbf{\$10,810} \end{aligned}$$

If we need to serve 1 MW of additional energy:

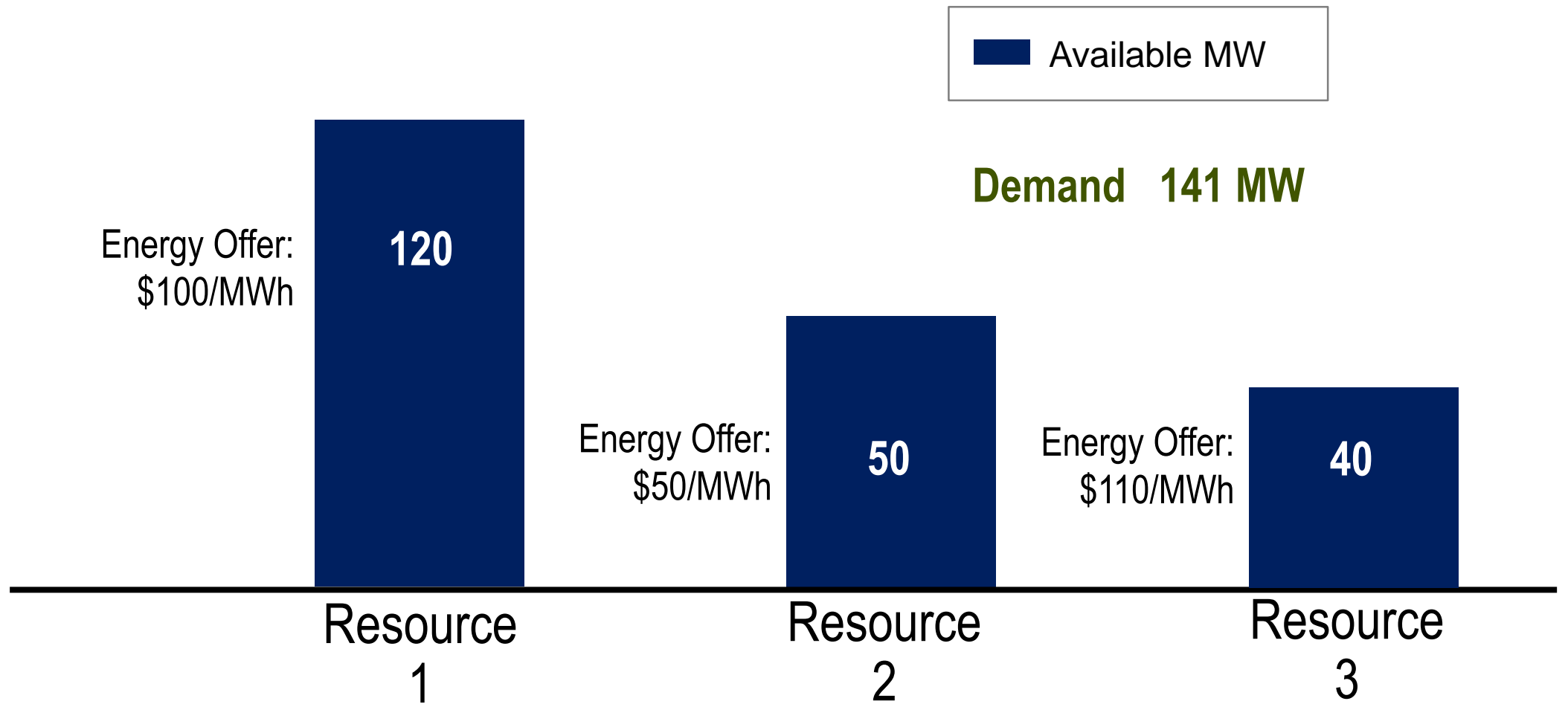
$$\begin{aligned} \text{Objective Function (+1MW)} &= (\$50/\text{MW} \times 50 \text{ MW}) + (\$100/\text{MW} \times \mathbf{92 \text{ MW}}) + (\$0 \text{ MW} \times 15 \text{ MW}) - \$790 \\ &= \mathbf{\$10,910} \end{aligned}$$

The change in the Objective function to serve 1 MW of additional energy is:

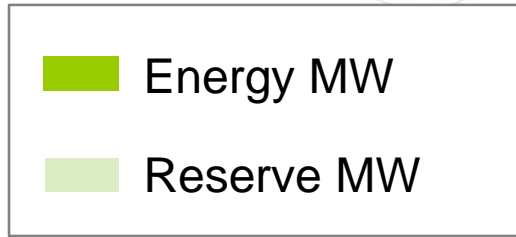
$$\begin{aligned} \text{Change in Objective Function} &= \$10,910 - \$10,810 \\ &= \$100 \end{aligned}$$

Therefore, the energy clearing price is \$100/MWh. Note that, **for this particular example**, the reserve price (\$35/MWh) **is not** added to the original energy-only price (\$100/MWh)

Example #4: Reserves Surplus



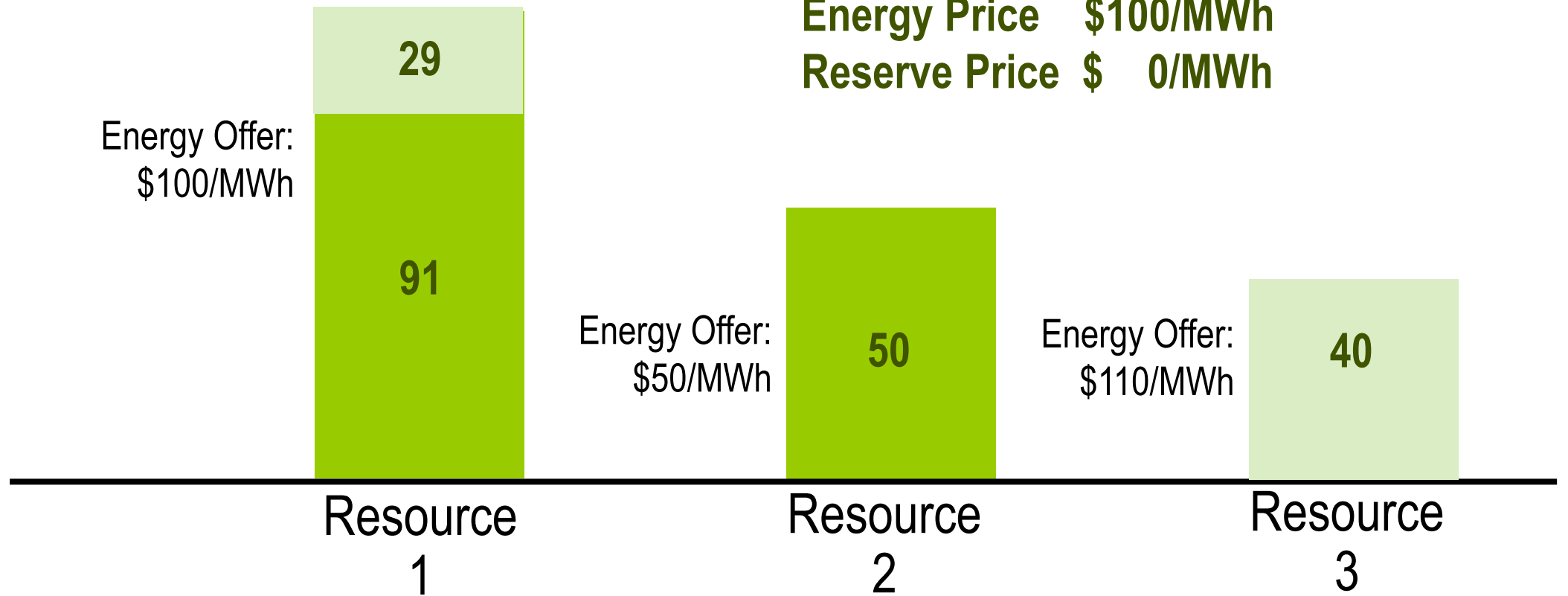
Example #4: Results



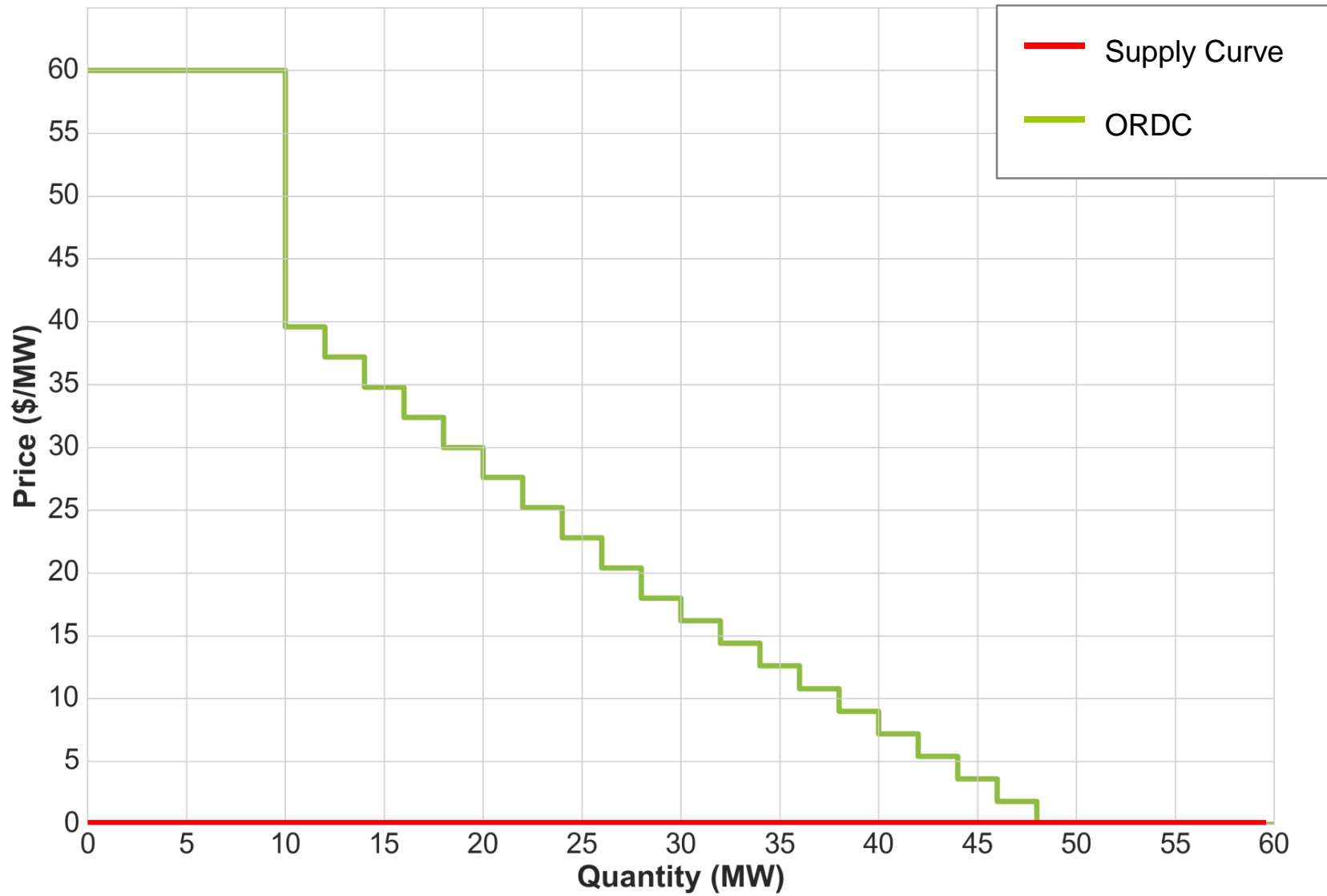
Demand 141 MW

Energy Price \$100/MWh

Reserve Price \$ 0/MWh



Example #4: Results - ORDC



Co-Optimizing Energy and Reserves – Example 4

Objective Function = cost to produce energy + cost to produce reserve – willing to pay for reserve

$$\begin{aligned} \text{Objective Function} &= (\$50/\text{MW} \times 50 \text{ MW}) + (\$100/\text{MW} \times 91 \text{ MW}) + (\$0 \text{ MW} \times 69 \text{ MW}) - \$1280 \\ &= \mathbf{\$10,320} \end{aligned}$$

If we need to serve 1 MW of additional energy:

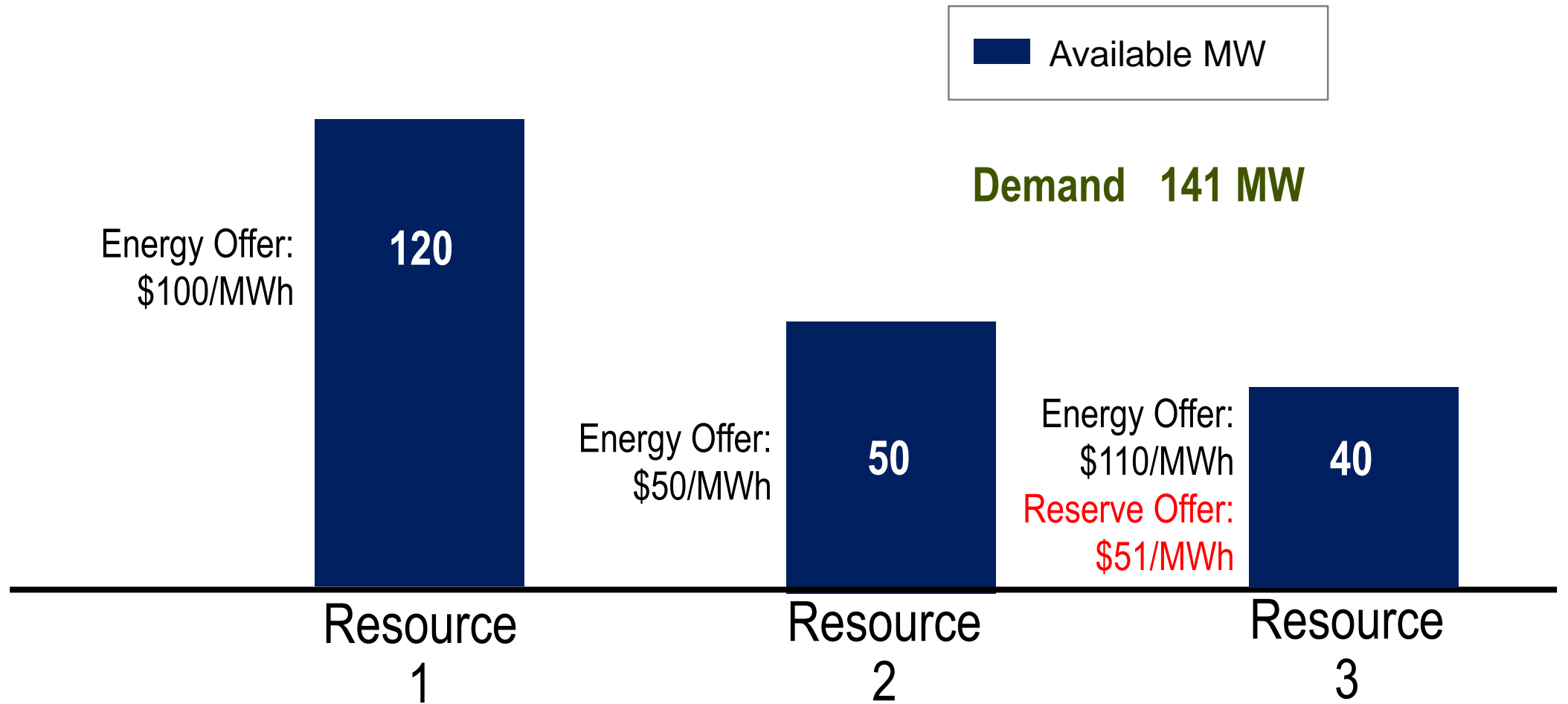
$$\begin{aligned} \text{Objective Function (+1MW)} &= (\$50/\text{MW} \times 50 \text{ MW}) + (\$100/\text{MW} \times \mathbf{92 \text{ MW}}) + (\$0 \text{ MW} \times \mathbf{68 \text{ MW}}) - \$1280 \\ &= \mathbf{\$10,420} \end{aligned}$$

The change in the Objective function to serve 1 MW of additional energy is:

$$\begin{aligned} \text{Change in Objective Function} &= \$10,420 - \$10,320 \\ &= \$100 \end{aligned}$$

Therefore, the energy clearing price is \$100/MWh. The reserve clearing price of (\$0/MWh) does not impact the original energy-only price (\$100/MWh)

Example #5: Reserves Economic Shortage

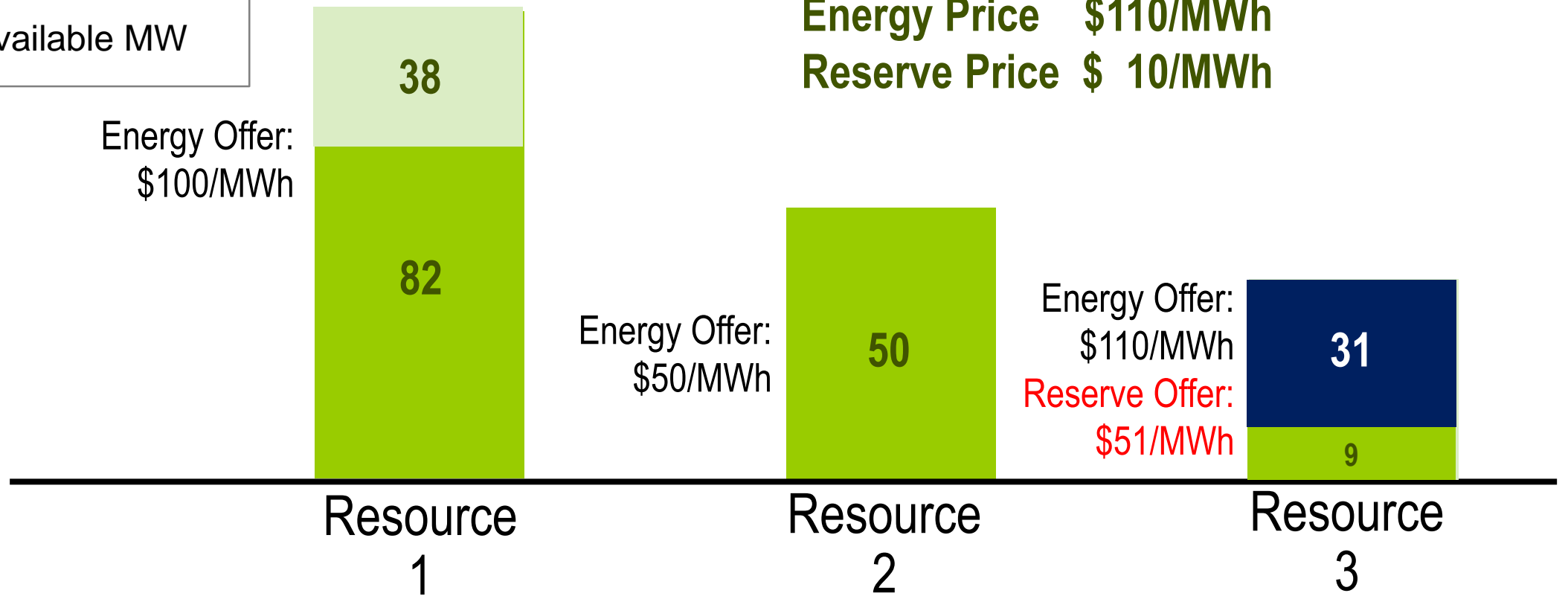


Example #5: Results

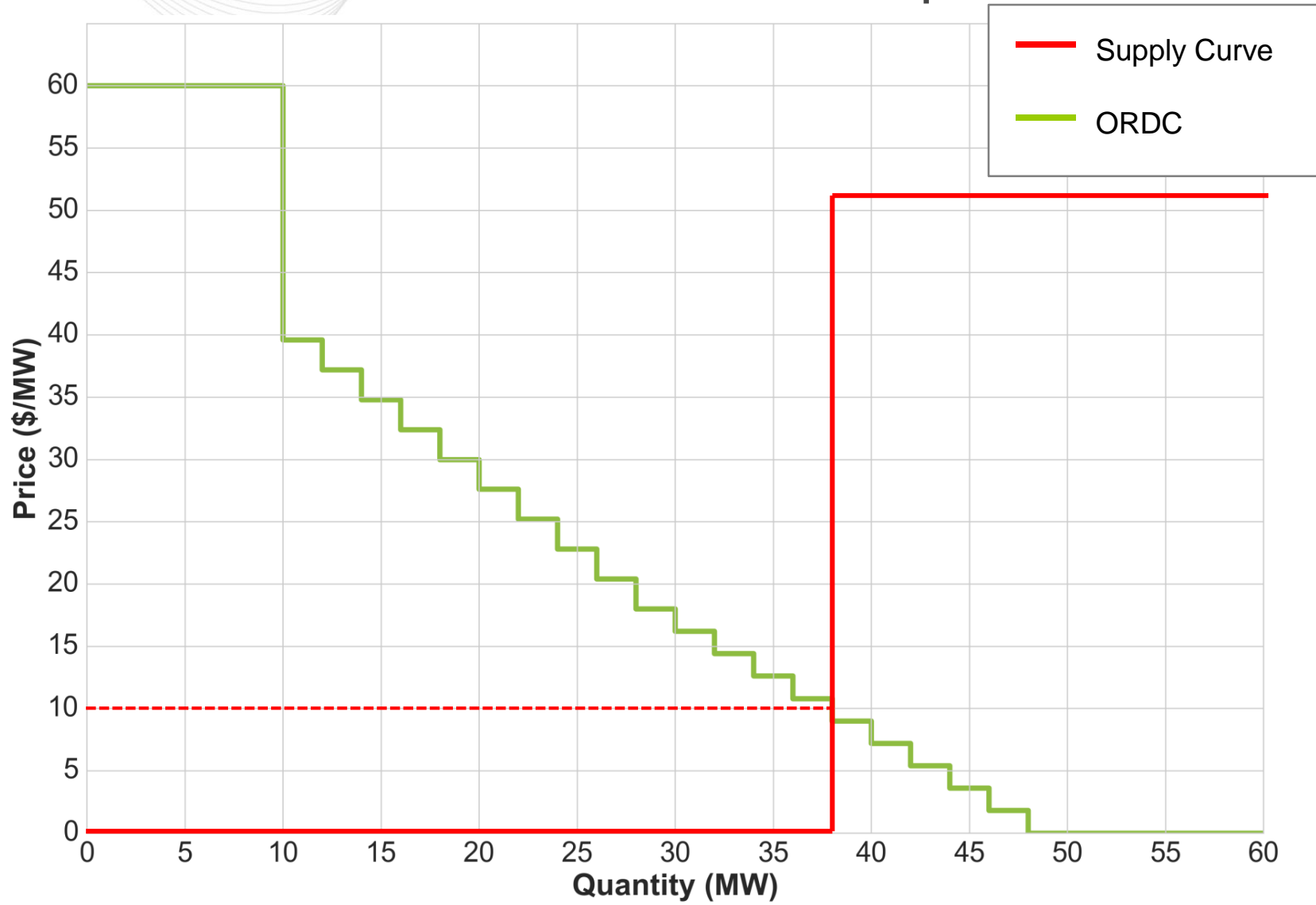


Demand 141 MW

Energy Price \$110/MWh
Reserve Price \$ 10/MWh



Example #5: Results - ORDC



Co-Optimizing Energy and Reserves – Example 5

Objective Function = cost to produce energy + cost to produce reserve – willing to pay for reserve

$$\begin{aligned} \text{Objective Function} &= (\$50/\text{MW} \times 50 \text{ MW}) + (\$100/\text{MW} \times 82 \text{ MW}) + (\$110/\text{MW} \times 9) + (\$0 \text{ MW} \times 38 \text{ MW}) - \$1250 \\ &= \mathbf{\$10,440} \end{aligned}$$

If we need to serve 1 MW of additional energy:

$$\begin{aligned} \text{Objective Function (+1MW)} &= (\$50/\text{MW} \times 50 \text{ MW}) + (\$100/\text{MW} \times 82 \text{ MW}) + (\$110/\text{MW} \times \mathbf{10 \text{ MW}}) + (\$0 \text{ MW} \times 38 \text{ MW}) - \$1250 \\ &= \mathbf{\$10,550} \end{aligned}$$

The change in the Objective function to serve 1 MW of additional energy is:

$$\begin{aligned} \text{Change in Objective Function} &= \$10,550 - \$10,440 \\ &= \$110 \end{aligned}$$

Therefore, the energy clearing price is \$110/MWh. The reserve clearing price of (\$10/MWh) does not impact the original energy-only price (\$110/MWh)

Resource 1 is indifferent to providing energy or reserves due to the co-optimization of energy and reserves

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